Statistics and the Ontario Lottery Retailer Scandal

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his paper describes the role simple statistical analysis played in exposing the Ontario lottery retailer scandal, which ended up becoming frontpage news in Canada and leading to numerous consequences including legislative debate, the firing of two CEOs, several criminal charges, jail time, and payouts totaling more than \$20 million. The story stands as a forceful testament to the importance and power of statistics.

How It All Started

I am primarily a theoretical statistics researcher, but after publishing a successful general-interest book about probabilities, I did a lot of public speaking and media interviews, especially in Canada. I was interviewed about such things as crime statistics, pedestrian death counts, decisionmaking, game show strategies, hockey forecasts, lottery jackpot probabilities, calculating risk, contests, election polls, and more.

Because of this, I was approached in the summer of 2006 by Harvey Cashore and Linda Guerriero, producers for the investigative journalism television program "The Fifth Estate" on the CBC (i.e., the Canadian Broadcasting Corporation, Canada's national broadcaster, modeled after the BBC in the UK). They requested my help with a news story involving lottery fraud. I initially declined their request, since I was busy with other projects and was just leaving for a research trip to Europe. However, the CBC was unable to find an appropriate replacement, so they contacted me again upon my return, and I agreed to meet with them. Then, the more I heard about the case, the more interesting it sounded.

I was told the story of Bob Edmonds, a mild-mannered elderly gentleman from the small town of Coboconk, Ontario, Canada. He always played the same lottery numbers, but (like many players) he left it to the store clerk to check if he had won anything. On July 27, 2001, he brought two tickets to his local convenience store. One of these tickets won him a free ticket. which the clerk gave him. But the other ticket won him \$250,000, a fact the clerk kept to herself. The clerk later tried to claim the winning ticket as her own. Although the lottery company was suspicious, the clerk finally managed (after a few maneuvers, including a sneaky

meeting with Edmonds in which she convinced him to share his old tickets and reveal his lottery purchase patterns) to convince them to pay her the \$250,000.

When Edmonds heard about the clerk's win, he realized what had happened. He then spent the next 3.5 years struggling to convince the Ontario Lottery and Gaming Corporation (OLG), the Ontario Provincial Police, and, ultimately, a court judge of the merits of his case. He finally prevailed in March 2005, when the OLG agreed to pay him \$200,000 of his winnings, but only on the condition that he promises to keep his case confidential.

Edmonds' case is a tribute to one man's brave persistence in fighting for justice. The CBC then wondered if the OLG's insistence on confidentiality was motivated by concern about other possible similar cases. They asked me to examine related data from a statistical point of view.

Facts and Figures

So what did the numbers say? The CBC ascertained (through a Freedom of Information request) that there was a total of 5,713 major (i.e., \$50,000 or more) lottery wins in Ontario from 1999-2006. (This figure combines all the lotteries sold in Ontario, such as the biweekly Canada-wide "Lotto 6/49" that involves choosing six distinct numbers from 1 to 49, thus giving probability $1/(\frac{49}{6}) = 1/13, 983, 816$ of winning the jackpot.) Of these 5,713 major wins, about 200(3.5%) were recorded as being won by lottery retailers (i.e., people who worked in stores that sold lottery tickets). The OLG records were rather spotty, so even these basic facts had to be carefully assembled. Furthermore, retailer wins were only recorded if the lottery winner answered "yes" when the OLG asked if they worked at a store, so the true figure was probably even higher than 200.

Is 200 wins too many then became the question. How many of the 5,713 major prizes should we have expected these sellers to win? And, what are the odds they would win 200 or more of them honestly (i.e., by pure luck)?

To answer these questions, we first needed to know the total number of retail lottery sellers in Ontario. The OLG said they didn't know this figure, so we had to investigate on our own. We knew there were 10,300 lottery ticket sales locations in Ontario. Furthermore, a "The Fifth Estate" survey of 200 locations gave a sample average of 3.2 employees per location, with a sample standard deviation of 1.65. This gave a 95% upper limit of about $3.2 + 1.97 \times 1.65/\sqrt{200} = 3.43$ employees per location on average (i.e., fewer than 3.5), working out to $3.5 \times 10,300 = 36,050$ sellers in total.

We later learned that an OLG executive had testified in an unrelated court case that there were "50,000 or 60,000" such sellers, suggesting a new upper limit of 60,000 sellers. Adding to the confusion, just five days before "The Fifth Estate" program was to air, the OLG unexpectedly presented the CBC with a brand new table, now claiming a total of 140,000 sellers, which turned out on closer inspection to mean 101,000 active sellers plus 39,000 annual "turnover" (i.e., former employees, who weren't actually relevant since the issue was whether they were retailers at the time they won their prize). So, this suggested a new upper limit of 101,000 sellers (though this figure was probably inflated (e.g., it included huge numbers of grocery and pharmacy workers even though most of them don't actually handle lottery tickets). In our calculations, we considered all of these possible values.

We also needed to know how much these sellers spend on lottery tickets. Again, the OLG said they didn't know. So, "The Fifth Estate" survey asked about this, too. Of the 195 employees who responded, 131 said they played the lottery. Their self-identified amounts spent per year on lottery tickets had a sample mean of \$476 and sample standard deviation of \$602.50 (giving a mean standard error of \$602.50/ $\sqrt{131} = 52.64). Putting these facts together led to an upper limit on average retailer annual lottery spending that was approximately 1.5 times as much as the average annual lottery spending of all Ontario adults (including those who never play). (The OLG later conducted its own survey and got a fairly similar answer: 1.9. And Corporate Research Associates Inc. later studied this same question in Atlantic Canada and obtained a factor of 1.52, virtually identical to "The Fifth Estate" figure.)

Putting It All Together

From all of these numbers, what could we conclude? The first question was, how many of those 5,713 major lottery wins from 1999-2006 would we 'expect' retailers to win in the absence of any fraud or cheating? As a simple approximation, I figured the fraction of lottery prizes we would expect retailers to win should be equal to the fraction of all Ontario lottery tickets they buy, or (even simpler) the fraction of lottery ticket sales dollars spent by retailers. (This approach ignored such subtleties as precisely which types of lottery games were played by which people, but there was no indication that retailers played different types of games than anyone else, so I didn't worry about that issue.)

Of course, the answer to this question depended on which of the above employee counts we used, so we considered them all for completeness. If we used the upper limit of 60,000 sellers (from the OLG's court testimony), together with the spending factor of 1.5 (from "The Fifth Estate" survey), then since there was a total of about 8,900,000 adults in Ontario during the time period under review, it followed we would expect lottery sellers to win approximately

$$5,713 \times \frac{60,000 \times 1.5}{8,900,000} \doteq 57,$$

(i.e., about 57 of those 5,713 major prizes).

This figure of 57 is indeed far less than the 200 major prizes the Visit http:// chance.amstat. org/category/ supplemental for a teaching supplement.



retailers actually won. So, did that indicate cheating? Or, could the retailers have won so many prizes simply by chance? After all, lotteries are inherently random and anyone can get lucky and win. To consider this question, I needed a probability distribution for the number of prizes retailers would win in the absence of fraud or cheating.

I figured that since the number of retailer wins is the result of lots of different tickets, each having a very small probability of winning, this probability distribution should be well approximated by the famous Poisson distribution. So, the probability of the retailers winning 200 or more prizes by luck alone should be approximately equal to the probability that a Poisson distribution with mean 57 will give a value of 200 or more. This probability is easily computed (e.g., using R) and turns out to be unimaginably small: less than one chance in a trillion, trillion, trillion, trillion. (Of course, this probability assumes the figure of 57 is correct—that the imputed facts about retailer counts and spending patterns are correct—a subtlety that was sometimes forgotten in the ensuing reportage.)

Even taking the largest OLG estimates (i.e., 101,000 sellers spending an average of 1.9 times as much as the general adult population), we would still expect just 123 major wins by sellers over this time period. The probability of their winning 200 or more major prizes would then be less than one chance in 7 billion again absolutely inconceivable.

We also considered retail store owners (as opposed to other employees) as a separate group. Those owners won about 83 of the major wins between 1999 and 2006. We didn't know the precise number of retail store owners (and the OLG wouldn't say), but even under the most generous assumptions, we would expect at most 26 owner wins-far fewer than 83, which would again be extremely unlikely (less than one chance in a trillion trillion). This provided still more evidence of fraud, specifically regarding storeowners.

It was also possible to break down the retailer winners according to what type of store they worked at. Indeed, retailers working at independent convenience stores represented only about onefifth of all the lottery retailers, but won a much higher fraction of the retailer major prize wins. The OLG wouldn't tell the CBC precisely how many, but an OLG FAQ web page later admitted that 101 out of 190 identified insider wins, or 53%, were specifically from sellers at convenience stores. Once again, it was inconceivable that such a large number of wins could have arisen purely by chance, thus providing further evidence of fraud specifically at convenience stores.

So, no matter how you sliced it, it was clear that lottery sellers were winning significantly more major lottery prizes than could be accounted for by chance alone. The statistics had proved the existence of widespread lottery fraud. With that, I presented my detailed analysis to the CBC, congratulated myself on a simple consulting job well done, and moved on to other matters.

Making a Splash

"The Fifth Estate" episode finally aired on the evening October 25, 2006. That morning, even before air time, I woke up to see that this episode (shared in advance with other media by the CBC) had already become a huge news story. My statistical analysis was described on the front page of a national newspaper under the headline, "Lottery Insiders Win Big Bucks: Odds of Ontario Results Are Astronomical, Investigation by CBC Program Reports."

The story's statistical conclusions were a lead item on most Canadian television news broadcasts and newspapers that day and beyond, with headlines like "Lottery-Winning Retailers Beating Statistical Odds" and "Those Big Winnings May Have Been Yours." They were discussed in newspaper editorials with titles like "Another Lottery Gamble" and "Keep an Eye on Your Winnings." They were even picked up internationally (e.g., Reuters, a Freakonomics blog entry, and a Spanish blog). Hundreds of lottery customers posted in online forums to express outrage at having been potentially defrauded in this way, and I was flooded with media interview requests. For a few days, it seemed virtually everyone in Canada was discussing lottery retailer fraud and the statistical evidence involved.

Needless to say, this was the first time my statistical work became front-page news!

The issue also was debated in the legislature of the Ontario provincial government (which oversees the OLG). The government was peppered that day and the next with questions such as the following:

Robert W. Runciman (Leeds-Grenville): My question is for the Minister of Public Infrastructure Renewal. Minister, today there are disturbing reports that over the last several years more than 200 lottery insiders have won prizes in excess of \$50,000. Jeffrey Rosenthal, a U of T professor, says that it's "extremely unlikely" these insiders would hit the jackpot that many times. The story, which is going to air on "The Fifth Estate" tonight, suggests that two thirds of these insider wins may have involved deception. Minister, can you tell us when you became aware of this issue and whether or not you plan to investigate the matter to ensure that Ontarians are not being defrauded of their rightful winnings?

and

Peter Kormos (Niagara **Centre):** A question to the Minister of Public Infrastructure Renewal: I too want to ask you about those over 200 incredibly lucky Ontario lottery retailers who have won prizes worth more than \$50,000 each in the last seven years. The statistics indicate that they beat odds of a trillion trillion trillion to one. That's odds of one quindecillion to one. Why wouldn't that phenomenon in and of itself have rung alarm bells in the OLG, rather than waiting for the CBC to blow the whistle?

Needless to say, this was the first time my statistical work was a topic of legislative debate!

Responses and Consequences

At first, the OLG tried to refute the statistical findings. They denied there was significant lottery fraud, called the statistical analysis "simplistic," insisted that the Edmonds case was an "isolated" one, and hired their own statistical consultants in an attempt to discredit me. The OLG CEO, Duncan Brown, even stated on television that "what was missing from 'The Fifth Estate's' numbers was the frequency of play of the retailers," which was not only insulting but also completely false (as was clear from my report, which was available on the CBC website). This was the first time my statistical work was opposed so vigorously and publicly, which made me feel rather uncomfortable (and also gave me a grudging sympathy for politicians, who are publicly criticized so frequently). However, the OLG tactic had limited success due to the sustained customer outrage.

The Ontario ombudsman, in charge of investigating issues of concern that fall under the purview of the Ontario government, stepped in to investigate. A few months later, he issued his report, a scathing indictment of the OLG's "buddy-buddy" relationship with the retailers that caused it to turn a "blind eye" to questionable winnings because it was "fixated on profits rather than customer service." The report concluded, "Without question, insiders have won big over the years. ... [M]illions of dollars have been paid out in what are dishonest claims." The report, in turn, put additional pressure on the Ontario government, including calls for the relevant minister to resign. The government resisted such calls, but instead fired the OLG CEO. (Then again, the CEO had misleadingly insulted my statistical analysis, so I didn't mourn him for long.)

Needless to say, this was the first time my statistical work led to anyone getting fired!

On the positive side, the scandal caused the OLG to institute various policy reforms. The stores' ticket-checking machines must now be viewable by customers and make loud noises to indicate wins. Customers are now required to sign their name on their lottery tickets before redeeming them to prevent switches. New self-checker machines have been installed to allow customers to easily learn what they've won before handing their tickets to anyone else. And ticket sellers cannot purchase lottery tickets at their own store. All of these measures are designed to ensure that future customers cannot be cheated in the manner that Edmonds—and probably many others—were.

In addition, a forensic audit was conducted that concluded, as we suspected, retailers had actually won far more lottery prizes than was originally recorded. Also, the negative publicity prodded the OLG to pay Edmonds the remainder of his winnings and write him a formal letter of apology just days before he died of cancer on April 2, 2007.

My own involvement continued, with such activities as speaking at a Toronto Police Fraud Squad conference and being asked to write an article about lottery fraud for the Royal Canadian Mounted Police newsletter. Overall, the investigation led to policy reforms and exposing a number of important truths. I was pleased with the role statistics had played in bring this about and thought that would be the end of the story.

Moving Beyond Ontario

Repercussions of the story soon moved beyond Ontario. National press coverage caused customer outrage in British Columbia (BC), as well. Initial assurances that the lotteries in BC were "safe" were rightly questioned, and the ombudsman in that province launched his own investigation. Some months later, he concluded that there also were excessive retailer lottery wins there and their lottery system was "open to fraud by retailers trying to cheat customers." The BC government followed Ontario's lead by firing the president of the BC Lottery Corporation, thus bringing to two the number of CEOs felled by this statistical story. Under increased scrutiny, the number of retailer wins in BC later dropped.

The province of Nova Scotia provided another interesting case. When the Ontario story first broke, the Atlantic Lottery Corporation (ALC) defiantly declared that their system was "foolproof," saying, "At Atlantic Lottery, our retailers, our staff, none of the people involved in the sale of our products, has the potential to impact the outcome of any of our products."This surprised me since I saw no reason that the situation in Atlantic Canada would be fundamentally different from Ontario. And I wasn't the only one.

The Nova Scotia Gaming Corporation (NSGC), which had the role of overseeing the Atlantic Lottery Corporation within the province of Nova Scotia, hired me to get to the bottom of the situation there. I performed a similar analysis to what I had done in Ontario, concluding that Nova Scotia retail store owners had won 22 of 448 major (\$25,000+) lottery prizes during the period 2001–2006 (excluding seven that were already under investigation). By contrast, they would be expected to win just over one such prize. It was, again, inconceivable that these wins could have been by luck alone. So, once again, this provided convincing evidence of retailer fraud. (And 18 of the 22 wins were by independent convenience store owners, indicating once again that most of the problem was in that sector.)

These and related findings were reported and led to lottery policy reforms and further inquiries in Nova Scotia. It also was discovered that, in 2005, the ALC "hid" a retailer win to avoid suspicion. As a further consequence, the ALC withheld executive bonuses in 2007 and held up their CEO's new longterm contract.

Related developments occurred with the Western Canada Lottery Corporation, which oversees lottery operations in three Canadian provinces and three territories. They issued an auditor's report that cautiously reassured that "no evidence was found of a consumer complaint against a retailer location that corresponded to a prize or validation issue consistent with an identified or potential retailer employee major prize win." The CBC's Western Canada news bureau asked me to investigate this. I performed a brief analysis that concluded, yet again, that the number of retailer wins was too high. Retailers won 67 major (\$10,000+) prizes from 2003–2006, while their expected number of wins was at most 34, and the probability of this occurring by chance was extremely small. My analysis also broke down the results by province and found that the individual provincial retailer win counts were too high. My conclusions were reported by the CBC and caused the government and ombudsman in Manitoba to launch a review while attempting to reassure their customers.

Perhaps most interesting in the Western Canada case was my discovery of a fundamental error in the previous auditor's report. They had computed the expected number of retailer wins by multiplying the retailer count by the "greater play rate" of 1.9 (fair enough), but then dividing that not by the total adult population, but rather 75% of the adult population that plays lottery games. So, they were effectively counting the same 75% factor twice, which caused them to compute the expected number of retailer wins as 75% higher than it should have been (but still not as high as the actual number of retailer wins).

In the province of Québec, Lotto-Québec initially tried to assure their customers that they had no fraud problem. However, the lottery scandal story received extensive coverage there and led to a detailed television inquiry into possible Québec lottery retailer fraud. This, in turn, forced Lotto-Québec to bring in additional security measures to protect their customers.

Related cases also arose in the United States. An Arizona convenience store clerk was arrested for claiming a customer's \$1.5 million jackpot as her own, which a spokesperson for the Arizona Lottery insisted "has not happened before, and I doubt it will happen again." A shop worker in Grand Prairie, Texas, cashed in a customer's \$1 million winning lottery ticket before fleeing to Nepal. The Texas Lottery Commission refused to pay the rightful owner, although this was one of six suspected lottery fraud cases in Texas in 2008–2009.

In Iowa, the state ombudsman issued a report criticizing the Iowa Lottery for failing to protect customers from retailer fraud and said it had missed an opportunity to learn from the Ontario lottery scandal. And in California, the lottery company conducted an elaborate sting operation, reported in detail by NBC News. They created fake winning lottery tickets and had an undercover investigator bring them to be checked in various retail stores. While most retailers reacted honestly, some of them denied the tickets were winners and then later tried to claim the prizes themselves. They were arrested and charged with fraud.

The report suggested the problem also extended to other states. The Minnesota State Lottery then undertook a similar sting operation in 2009, as did the Ohio Lottery in 2010; both operations resulted in arrests.

It seemed that this was not just an Ontario issue after all.

Calling the Cops

The Ontario Ombudsman's report discussed, in addition to the statistical arguments, several specific cases in which lottery winnings had been paid out to retailers despite suspicious circumstances (such as the prize winner not being able to recall their lottery ticket purchase patterns). At first, it seemed these cases would remain as unsolved mysteries. Indeed, my statistical analysis could estimate the total number of fraudulent cases, but could not identify specific instances of fraud. However, the OLG was now taking these cases seriously. They collaborated with the Ontario Provincial Police to investigate in detail.

The first case was cracked when four Toronto friends realized their jointly purchased lottery ticket from June 2004 had won a \$5.7 million prize, which they had not received. They initially accused each other of theft (thus ruining their friendship), before finally realizing the retailer was to blame. After an investigation, convenience store owner Hafiz Malik was arrested and charged with fraud for cashing in their winning ticket in January 2005. Malik confessed and pled guilty in December 2009, receiving a one-year prison sentence. The four winners were paid in full, plus interest, for a total payout of \$6.5 million from the OLG.

Another case involved a woman who had no idea she was a winner until the OLG carefully tracked her down. Javed Nazami, the manager of a Burlington convenience store, was charged with fraud and theft for stealing her winning November 2004 lottery ticket and cashing it in. The OLG paid the woman the full value of her winnings (this time "only" \$80,000, or \$94,000 with four years of accumulated interest).

The most dramatic case involved a \$12.5 million winning ticket from December 2003, which was cashed by the daughter of a convenience store owner two months later. The daughter originally denied she was related to a retailer, but could not provide details about where she purchased the ticket. The OLG waited for nearly a year before secretly paying the prize. This case was flagged as suspicious in the ombudsman's report and later investigated in detail by the CBC's "The Fifth Estate"-including a secretly recorded interview with the father who seemed to suggest that if no one can prove fraud, then "finders keepers" prevails.

There was then no further news about this case for 3.5 years. So, I was very surprised in September 2010 when the father and daughter and another sibling were arrested and charged with theft. In this case, the OLG had determined that the prize was paid to the wrong people, but they did not know whom the true winners were. In a dramatic move, the police and OLG publicly announced that they were "seeking" the rightful winner and invited applications from potential winners. Not surprisingly, they received hundreds of claims, which they then attempted to sort though and investigate. Finally, in January 2011, a group of seven construction workers who applied late in the process were able to answer all questions about their lottery-buying habits correctly and were awarded the \$12.5 million (or \$14.8 million with interest).

Needless to say, this was the first time my statistical work had led to criminal charges, jail time, or multimillion-dollar payments!

Reflections

Looking back, I am rather amazed at how the lottery retailer scandal story unfolded. I never expected this issue to become so big, or to have such wide repercussions: Edmonds was vindicated, customers across the country were outraged, the lottery company was on the defensive, politicians debated, CEOs were fired, criminal charges were laid, people were sent to jail, and more than \$20 million was paid.

Of course, many forces were required to move the story along: Edmonds' persistence, the CBC "The Fifth Estate's" investigative journalism, the ombudsman's detailed report, extensive police scrutiny, the OLG's later cooperation and analysis, and more. But statistical analysis also played a major role in broadening the issue from a specific case into a widespread concern. This was nicely summarized in a later *Toronto Sun* article, which began:

For a guy who has never bought a lottery ticket at a corner store, Jeff Rosenthal has sure hit it big. And lottery corporations across Canada would likely wish he would just stop playing their numbers so well. Since 2006, the Toronto math professor has been the brain behind uncovering a suspected massive theft of lottery winnings by sticky fingered store clerks. The ripple effects of his seemingly innocuous number crunching—figuring, on behalf of the CBC, the likely odds of so many retailers routinely becoming winners—has led to the greatest scandal in the history of Canadian lotteries.

I could not have put it any better myself.

Further Reading

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About the Author

Jeffrey Rosenthal is a professor in the department of statistics at the University of Toronto. He earned his BSc from the University of Toronto and his PhD in mathematics from Harvard University. He received the 2006 CRM-SSC Prize, the 2007 COPSS Presidents' Award, the 2013 SSC Gold Medal, and teaching awards at both Harvard and Toronto. He is a fellow of the Institute of Mathematical Statistics and Royal Society of Canada. Rosenthal's book for the general public, *Struck by Lightning: The Curious World of Probabilities*, was a bestseller in Canada, leading to numerous media and public appearances. He also dabbles in computer game programming, music performance, and improvisational comedy. His website is www.probability.ca.